

## ② Phase of Resonance :

$$\text{W.K.T. } \tan \alpha = \frac{A}{B}$$

$$\tan \alpha = \frac{\mu P}{k - m\omega^2}$$

$$\tan \alpha = \frac{\mu P}{\frac{k}{m} - \omega^2} \quad \text{--- ①}$$

② Here  $\alpha$  is phase difference between natural frequency and resultant forced frequency

$$\text{At resonance } \frac{k}{m} = \omega^2$$

$$\Rightarrow \omega = \omega_p$$

So eq<sup>n</sup> ① becomes

$$\tan \alpha = \frac{\mu P}{\cancel{\frac{k}{m}} - \cancel{\omega^2}}$$

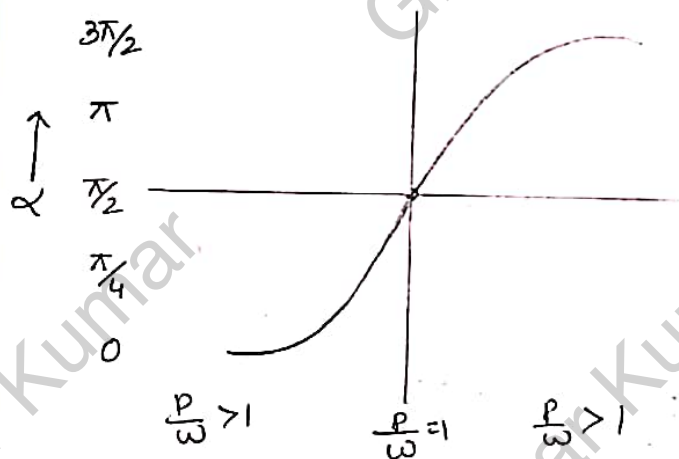
$$\tan \alpha = \infty$$

$$\alpha = \tan^{-1}(\infty)$$

$$\alpha = \frac{\pi}{2}$$

This means that at resonance ~~phase~~ the phase difference is 90°

If we draw the graph  $\alpha$  v/s  $\frac{p}{\omega}$ , then we will get the graph as shown in below



$$\text{For } \frac{p}{\omega} = 1, \quad \alpha = \frac{\pi}{2}$$

$$\frac{p}{\omega} < 1, \quad \alpha < \frac{\pi}{2}$$

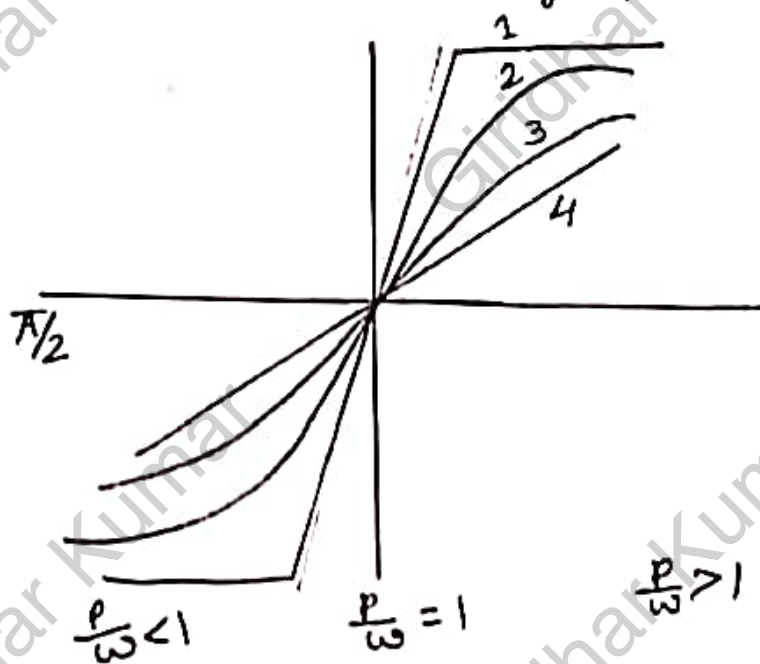
$$\frac{p}{\omega} > 1, \quad \alpha > \frac{\pi}{2}$$

### ③ Effect of damping on the phase of forced vibration:

We have the eq<sup>n</sup>,  $\tan \alpha = \frac{\mu P}{\left(\frac{k}{m} - p^2\right)}$  — (1)

In above eq<sup>n</sup>  $\alpha$  is the phase difference  
From the above eq<sup>n</sup> we can see that  
 $\alpha$  is directly proportional to  $\mu$ .

Let us consider a graph  $\alpha$  v/s  $\frac{p}{\omega}$



- When  $\mu$  is very less than we will get the curve (1)
- When  $\mu$  is medium then we will get the curve (2)
- When  $\mu$  is sufficiently high we will get the curve (4) as shown in the above graph.
- Although the phase difference  $\alpha$  will be  $\frac{\pi}{2}$  when  $\frac{p}{\omega}$  is equals to 1 or  $p = \omega$  (forced frequency = natural frequency)